

Math Buddy Teaching: A Best Practice for Supporting English Learners in Mathematics

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Abstract:

This study investigates the effectiveness of Math Buddy Teaching as a promising instructional strategy for enhancing mathematics learning among English Language Learners (ELLs). Through a systematic review of scholarly literature and relevant empirical research, the paper examines how this peer-based model supports students' conceptual understanding, language development, and engagement in multilingual mathematics classrooms. The Math Buddy Teaching approach integrates cooperative learning, peer-to-peer interaction, and language scaffolding, creating opportunities for learners to co-construct mathematical meaning through social interaction. Findings suggest that this model reduces language-related barriers by allowing students to process mathematical vocabulary and concepts in more accessible and culturally familiar ways. It also promotes academic confidence, encourages active participation, and contributes to a more inclusive and equitable classroom environment. Grounded in sociocultural and constructivist theories of learning, Math Buddy Teaching emphasizes the importance of social context, cultural knowledge, and learner agency in the construction of mathematical understanding. As linguistic and cultural diversity continues to grow in educational settings, this model offers a viable and adaptable strategy for improving instructional equity and student achievement in mathematics education.

Keywords: Math Buddy Teaching, English Language Learners (ELLs), mathematics education

Introduction:

English Language Learners (ELLs) face unique and multifaceted challenges when engaging with mathematics, a subject that requires both conceptual reasoning and academic language proficiency. Mathematical tasks often demand a command of specialized vocabulary, syntax, and symbolic representation, placing ELLs at a distinct disadvantage in comparison to native English speakers (Abedi & Lord, 2001; Barwell, 2005). The difficulty lies not only in understanding mathematical procedures but also in decoding complex word problems, following verbal instructions, and articulating reasoning during class discussions (Adler, 1998; Brown, Cady, & Taylor, 2009).

The intersection of language and mathematics is a critical site for instructional reform, especially in linguistically diverse classrooms. Scholars have long emphasized that mathematics is not a "language-neutral" subject, as it requires students to engage in reading, writing, speaking, and listening with precision (Adams, 2003; Altieri, 2009).

For ELLs, these demands often result in limited participation and lower achievement, despite their potential mathematical competence. As Barwell (2011) notes, solving mathematical problems requires not only numerical understanding but also access to the language of instruction, highlighting the importance of strategies that integrate language development with math learning.

To address these barriers, educators have turned to peer-mediated strategies such as Math Buddy Teaching—a cooperative learning model in which students work in pairs to solve problems, explain concepts, and support each other's understanding. This approach has been shown to foster academic discourse, encourage mathematical reasoning, and build social connections that are particularly beneficial to ELLs (Franke, Kazemi, & Battey, 2007; Anthony & Walshaw, 2007). By engaging in reciprocal teaching and peer scaffolding, students are able to negotiate meaning and clarify mathematical ideas in ways that traditional instruction may not facilitate.

Moreover, Math Buddy Teaching aligns with cognitive and sociocultural theories of learning, which emphasize the value of interaction, dialogue, and shared problem-solving in constructing knowledge (Campbell, Adams, & Davis, 2007; Cobb & McClain, 2004). When implemented effectively, this practice can reduce linguistic isolation and foster a sense of inclusion among ELLs. As Clarkson (2007) found, bilingual learners often rely on both their native language and English when working with peers, enriching their mathematical thinking through multilingual resources. Such collaborative environments are especially powerful in promoting confidence and engagement among language learners.

This paper investigates Math Buddy Teaching as a best practice for supporting English Language Learners in mathematics classrooms. Drawing on recent research and theoretical perspectives, it explores how peer interaction, language-rich discourse, and cooperative problem-solving can help overcome linguistic and cognitive barriers in math education. Ultimately, the goal is to highlight evidence-based strategies that make mathematics more accessible, equitable, and meaningful for all learners, particularly those navigating the dual challenge of language acquisition and mathematical understanding.

Review of Related Literature:

Mathematical language presents a significant barrier to English Language Learners (ELLs), who must navigate both content mastery and linguistic comprehension simultaneously. According to Kenney (2005), mathematics is a language in itself—dense with abstract symbols, discipline-specific vocabulary, and complex sentence structures.

This abstraction often becomes a stumbling block for ELLs, who struggle not only with numerical concepts but also with decoding instructions, word problems, and the meaning embedded in mathematical discourse (Ferrari, 2004; Brown, Cady, & Taylor, 2009). Research by Abedi and Lord (2001) indicates that language factors in mathematics assessments can significantly skew performance outcomes for ELLs. Similarly, Kazima (2007) and Kaplan, Fisher, and Rogness (2009) highlight how lexical ambiguities and vocabulary misinterpretations in math problems exacerbate the challenges ELLs face.

In response, integrating literacy strategies into math instruction has been widely recommended. Scholars such as Adams (2003), Benjamin (2011), and Altieri (2009) advocate for reading and language-focused practices in mathematics classrooms, emphasizing the need for students to engage with both the symbols and the language of math.

Goldenberg (2008) and Hoffert (2009) further argue that effective mathematics instruction for ELLs must include explicit vocabulary instruction, use of visual aids, and structured opportunities for oral language use. Drawing from Halliday's (1978) theory of language as a social semiotic, educators are encouraged to treat mathematical communication as a socially constructed process. Thus, linguistic access to mathematical content is not a separate goal but an integral part of math learning itself.

Peer-assisted strategies like Math Buddy Teaching are grounded in Vygotsky's sociocultural theory, which views learning as a socially mediated activity. Forman (2003) and Franke and Kazemi (2001) explore how communities of practice facilitate the co-construction of knowledge in mathematics classrooms. Within these communities, peer dialogue serves as both a cognitive and linguistic scaffold, especially in bilingual and multilingual settings (Clarkson, 2007; Civil, 2007). Research by Fasi (1999) and Dawe (1983) confirms that students working in pairs or groups benefit from peer explanation, rephrasing of problems, and collaborative sense-making, which enhance both language development and mathematical reasoning. In particular, Franke, Kazemi, and Battey (2007) emphasize that such collaborative strategies are especially useful when adapted for ELLs, whose diverse linguistic backgrounds can enrich classroom discourse.

Math Buddy Teaching becomes even more relevant when instructional designs acknowledge and incorporate students' cultural and linguistic assets. Cobb and McClain (2004), along with Civil (2007), stress the importance of designing learning environments that are inclusive of students' lived experiences and community knowledge.

Frankenstein (1995) and Dunn (2005) argue that culturally responsive pedagogy in math enables marginalized learners to see their identities reflected in the curriculum, which in turn fosters engagement and equity. These arguments align with Confrey and Smith's (1995) work on making mathematical content meaningful by connecting it to real-life applications and students' prior knowledge. Moreover, Emerson, Fretz, and Shaw (1995) and Erickson (1986) advocate for ethnographic approaches in educational research to understand how students interact with content, peers, and language in authentic settings.

In addition, teacher training and professional development play a vital role in the successful implementation of Math Buddy Teaching. Desimone, Smith, and Ueno (2006) found that teachers often lack sustained, content-specific training necessary to support diverse learners. Kasmer (2013) and Cobb et al. (2003) note that institutional factors, such as curriculum mandates and school policies, influence teachers' ability to adopt innovative pedagogies.

Therefore, for Math Buddy Teaching to be effective, educators must be equipped with both theoretical understanding and practical tools to facilitate peer-based learning. Empson (2003) and Fuchs et al. (1998) provide evidence that such instructional innovations, when implemented with fidelity, can significantly improve outcomes for low-performing and linguistically diverse students. Finally, Flores (2007) and Ferguson (1998) remind educators of the broader systemic inequities that shape educational access and achievement, underscoring the need for strategies like Math Buddy Teaching that promote both academic and social inclusion.

The literature strongly supports the integration of peer-assisted learning, cultural responsiveness, and language-focused strategies in mathematics instruction for English Language Learners. Math Buddy Teaching, situated within this theoretical and empirical framework, emerges as a promising practice that not only enhances comprehension and participation but also fosters a more equitable learning environment. Future research and practice should continue to explore how this approach can be scaled and adapted across diverse educational contexts.

Methodology:

This qualitative study employed a systematic review methodology to synthesize existing research on English Language Learners (ELLs) and mathematics instruction. The review focused specifically on literature published in peer-reviewed journals, educational research monographs, and empirical studies that explore the intersection of language acquisition, mathematics learning, and instructional strategies. The selection criteria prioritized studies that addressed peer collaboration, language development, conceptual understanding, and culturally responsive teaching practices in mathematics education.

A comprehensive search strategy was implemented using academic databases such as ERIC, JSTOR, and Google Scholar. Keywords included combinations of terms such as "English Language Learners," "mathematics instruction," "peer-assisted learning," "language scaffolding," and "culturally responsive pedagogy." Studies were selected based on their methodological rigor, relevance to classroom practices, and their contributions to understanding how ELLs engage with mathematical content in diverse educational settings.

The data analysis process involved qualitative coding of findings, arguments, and instructional practices discussed in the reviewed studies. An inductive approach was used to identify emerging patterns and recurring concepts. These codes were then organized into broader thematic categories: (1) Language Scaffolding, which explores how linguistic support strategies enhance mathematical understanding; (2) Social Interaction, which focuses on the role of collaborative learning and peer dialogue; (3) Conceptual Understanding, highlighting approaches that promote deep comprehension of mathematical ideas among ELLs; and (4) Classroom Equity, examining how inclusive practices address disparities in learning opportunities and outcomes.

By categorizing findings into these themes, the study aims to offer a synthesized understanding of effective strategies that support ELLs in mathematics classrooms. The systematic review not only identifies pedagogical gaps but also informs educators and policymakers seeking to enhance both language development and academic achievement through inclusive, research-informed instruction.

Findings and Discussion:

Language Scaffolding:

One of the central themes that emerged from the literature is the critical role of language scaffolding in supporting English Language Learners (ELLs) in mathematics classrooms. Language scaffolding refers to instructional strategies that assist learners in bridging their current language proficiency to the demands of academic language, particularly the specialized vocabulary and discourse of mathematics.

Research indicates that peer collaboration plays a vital role in this scaffolding process. Buddies or peer tutors can provide real-time support by rephrasing complex mathematical terms, explaining concepts in simpler language, and offering immediate feedback (Barwell, 2005; Boero, Douek, & Ferrari, 2008). This dynamic promotes not only linguistic development but also conceptual understanding, as students engage in dialogue that makes abstract ideas more accessible. Ferrari (2004) emphasizes that mathematical language is not merely about vocabulary but also about developing cognitive tools that allow students to think mathematically. Through structured peer interaction, ELLs can gradually internalize this language.

Early studies such as Dawe (1983) and Fasi (1999) explored bilingualism's role in mathematical reasoning, showing that students who could discuss math in both their first language and English exhibited greater flexibility and problem-solving skills. When teachers allow the use of students' home languages for collaborative problem-solving, learners can better grasp complex content and later transition into English mathematical discourse with greater confidence.

From a sociocultural perspective, Halliday (1978) described language as a social semiotic system, meaning that language use in context is integral to meaning-making. In mathematics classrooms, where precision and logic dominate, scaffolding through meaningful interaction is essential. Goldenberg (2008) adds that effective language scaffolding involves structured dialogue, where ELLs are given both the opportunity and the support to use mathematical language actively, not passively.

Moreover, language scaffolding is particularly important in decoding and comprehending word problems, which often pose unique challenges due to lexical ambiguity and syntactic complexity. Kaplan, Fisher, and Rogness (2009) found that many ELLs struggle with statistical and mathematical terms that have multiple meanings in everyday English—words like “average,” “random,” or “confidence” can be misleading. Teachers who explicitly address such ambiguities and model how to parse word problems can significantly reduce misunderstanding and build confidence.

Franke, Kazemi, and Battey (2007) suggest that creating spaces for mathematical discourse allows learners to make connections between everyday experiences and academic content. In this context, scaffolding involves more than just simplifying language; it includes asking open-ended questions, prompting students to explain their reasoning, and encouraging metacognitive reflection. This approach builds both language and higher-order thinking skills. Kenney (2005) reinforces this view, arguing that mathematics should be taught as a language in itself—with its own grammar, syntax, and meaning structures.

In multilingual classrooms, scaffolding must also include an awareness of cultural and linguistic backgrounds. Civil (2007) and Dunn (2005) advocate for culturally responsive teaching that recognizes students' home languages and cultural knowledge as assets, not barriers. For instance, ELLs may use culturally grounded metaphors or analogies when discussing mathematical ideas with peers. Rather than correcting these expressions, teachers should explore and validate them as part of the learning process, linking them to formal mathematical terms.

Effective scaffolding also relies on the teacher's ability to differentiate instruction and provide multiple entry points for learning. Fuchs et al. (1998) found that when teachers combined cooperative learning with formative assessment and explicit language instruction, ELLs made significant gains in both computation and problem-solving tasks. This aligns with Hoffert's (2009) argument that mathematics, while often considered a “universal language,” is anything but universal for students who lack fluency in the language of instruction. Instead, it must be demystified through targeted, student-centered support.

Another essential element of language scaffolding is the visual and symbolic representation of ideas. Kazima (2007) demonstrated that students in Malawi often misunderstood probability vocabulary because the terms lacked clear

visual referents. By using diagrams, number lines, graphs, and manipulatives alongside verbal explanations, teachers can bridge the gap between concrete experiences and abstract reasoning.

Kasmer (2013) noted that pre-service teachers in English-medium Tanzanian schools found success using gestures, visual cues, and graphic organizers to scaffold lessons for ELLs. These multimodal strategies helped compensate for language barriers and fostered student participation. Similarly, Confrey and Smith (1995) emphasized the importance of using real-world contexts and representations to scaffold exponential function instruction, highlighting how language, context, and representation work together to support learning.

Scaffolding is not a one-size-fits-all approach. As Desimone, Smith, and Ueno (2006) argue, effective implementation depends on sustained, content-focused professional development. Teachers must be trained not only in mathematics pedagogy but also in language acquisition and second-language instruction. Without this preparation, attempts at scaffolding may remain superficial or inconsistent.

Finally, the concept of equity must underpin all scaffolding efforts. Frankenstein (1995) and Flores (2007) highlight that linguistic support is a matter of justice: when students are denied access to meaningful math instruction due to language limitations, systemic inequities are reinforced. Language scaffolding, therefore, is both a pedagogical strategy and a commitment to equity and inclusion.

In conclusion, the literature underscores that language scaffolding is fundamental to supporting ELLs in mathematics. Through peer interaction, cultural responsiveness, visual aids, and explicit instruction, students can build both their language proficiency and their mathematical understanding. Educators must see scaffolding not as remedial, but as essential to developing confident, competent learners who are equipped to engage with mathematics as a dynamic and expressive language.

Cognitive Support:

Peer explanation has been widely recognized as a powerful cognitive support mechanism in mathematics education, especially for students learning in a second language. As Campbell, Adams, and Davis (2007) assert, peer explanation enhances metacognitive awareness and helps learners bridge conceptual gaps, allowing them to refine their understanding of mathematical concepts through collaborative dialogue. This support becomes particularly crucial for English language learners (ELLs), who often grapple with the dual challenge of learning both mathematical content and the academic language in which it is delivered.

Research underscores that mathematics, while often labeled a "universal language," is far from neutral or easily accessible to all learners (Kenney, 2005; Hoffert, 2009). Mathematical discourse relies heavily on precise language, symbols, and vocabulary that may not have direct equivalents in a student's first language, posing additional barriers to comprehension. In such contexts, peer explanation facilitates meaning-making by providing students the opportunity to articulate their reasoning, receive immediate feedback, and adjust their thinking in real-time. Through social interaction, learners negotiate meaning, clarify misunderstandings, and reinforce both content knowledge and language skills.

Dawe (1983) and Fasi (1999) both observed that bilingual learners benefit from the chance to use their first language as a tool to scaffold mathematical reasoning. When students are encouraged to explain their thinking to peers—whether in English or their native language—they access deeper levels of understanding and improve their metacognitive skills. Peer explanation encourages learners to verbalize their problem-solving processes, which supports the internalization of mathematical structures and logic.

Ferrari (2004) emphasizes that mathematical language is not merely a tool for communication but a structure that shapes thought itself. Thus, peer explanations help students internalize this structure by forcing them to translate abstract mathematical representations into coherent verbal explanations. This practice nurtures both linguistic and conceptual development, particularly for students whose cognitive growth is supported through interaction and discourse.

From a sociocultural perspective, Vygotsky's theory of the Zone of Proximal Development (ZPD) reinforces the importance of social interaction in cognitive development. Peer explanation is an enactment of this principle—students working slightly above their current level of competence can scaffold each other's understanding. Civil (2007) and Forman (2003) further support this idea, highlighting how mathematics learning is deeply embedded in communities of practice where language, symbols, and shared meaning evolve through interaction. Within this community, students co-construct knowledge, thereby enhancing both their mathematical proficiency and their language fluency.

Goldenberg (2008) and Kazima (2007) suggest that vocabulary acquisition in mathematics must be deliberate and contextualized. Words such as “average,” “random,” or “confidence” often carry specific mathematical meanings that differ from everyday usage, contributing to lexical ambiguity (Kaplan, Fisher, & Rogness, 2009). Peer explanations help demystify such terminology, as students restate definitions in their own words and situate them within concrete examples. This iterative process is especially valuable for second-language learners who must constantly navigate between colloquial and academic meanings.

Moreover, studies have shown that peer-assisted learning can be especially effective in heterogeneous classrooms. Fuchs et al. (1998) found that cooperative and peer-based learning environments not only improve mathematical competence but also foster positive interdependence among students. These environments encourage learners to value diverse perspectives, normalize struggle, and share ownership of learning outcomes. As noted by Erickson (1986), such ethnographic insights are essential in understanding how classroom discourse and peer dynamics influence individual cognition.

In practice, facilitating peer explanation requires intentional instructional strategies. Teachers must structure opportunities for discussion, model appropriate mathematical language, and foster a classroom culture where errors are seen as learning opportunities. Franke and Kazemi (2001) describe effective classrooms as those where teaching is treated as learning within a community of practice. In such environments, students not only receive cognitive support from peers but also develop a disposition toward collaborative inquiry and mutual respect.

Importantly, the effectiveness of peer explanation depends on the sociolinguistic context of the classroom. As Frankenstein (1995) and Dunn (2005) argue, equity in mathematics education involves recognizing and valuing the diverse cultural and linguistic backgrounds that students bring. Peer explanation allows these backgrounds to become resources rather than deficits, providing a culturally responsive framework for learning. When students explain ideas to peers who share similar linguistic or cultural experiences, they can more easily access prior knowledge and apply it to new mathematical situations.

Peer explanation is a vital cognitive support in mathematics education. It enhances metacognitive awareness, promotes conceptual clarity, and provides an inclusive pathway for ELLs and other marginalized learners to succeed. By embedding peer explanation within a culturally responsive and linguistically supportive environment, educators can foster both mathematical understanding and academic language development in a meaningful and equitable way.

Social Engagement:

Social engagement plays a critical role in shaping students' mathematical understanding, particularly for English Language Learners (ELLs) and culturally diverse learners. When students are immersed in collaborative learning environments that value their voices, languages, and cultural identities, their anxiety tends to decrease, and their sense of belonging increases. Research by Hoffert (2009) and Goldenberg (2008) underscores that safe, inclusive, and interactive classrooms support ELLs in overcoming linguistic barriers and building confidence in mathematical tasks. Collaborative learning not only provides cognitive scaffolds but also creates meaningful spaces for dialogue and negotiation of meaning, which are vital for mathematical reasoning and academic identity formation.

Mathematics, often perceived as a universal language, can serve as a powerful tool for social connection when taught through interactive and student-centered approaches. Kenney (2005) emphasizes that treating mathematics as a language entails recognizing its symbolic, logical, and representational nature. However, for students navigating mathematics in a second language, the social context in which they learn becomes even more crucial. Halliday's (1978) notion of language as a social semiotic underscores how language constructs meaning in social settings—this

applies directly to math classrooms where students use linguistic resources to articulate reasoning, justify solutions, and participate in shared problem-solving.

Social engagement enables students to actively construct knowledge with peers through discourse and group exploration. According to Franke, Kazemi, and Battey (2007), effective math instruction involves facilitating communities of practice where learners are encouraged to discuss strategies, analyze mistakes, and build collective understanding. In such environments, errors are reframed as learning opportunities rather than failures, fostering a growth mindset and deeper cognitive engagement. This social constructivist approach, rooted in Vygotsky's sociocultural theory, positions peer interaction as fundamental to internalizing abstract mathematical ideas.

Studies in bilingual and multilingual contexts have shown that social engagement is especially important for students learning mathematics in English as a second language. Dawe (1983) and Fasi (1999) found that when learners are encouraged to use their home languages alongside English in mathematical discussions, they are more likely to understand complex concepts and express their thinking clearly. Allowing multiple languages in math discourse not only affirms students' identities but also reduces cognitive load, as learners can process information in familiar linguistic frameworks before translating it into academic English. This form of inclusive pedagogy is a direct extension of equity in education, as discussed by Civil (2007), who argues that tapping into community knowledge and students' cultural funds of knowledge enriches classroom dialogue and engagement.

Furthermore, the use of culturally responsive tasks that reflect students' lived experiences enhances social participation and motivation. Frankenstein (1995) and Dunn (2005) emphasize the role of equity-oriented teaching that connects mathematical content with students' sociopolitical realities. When learners see themselves reflected in problem contexts and feel that their contributions matter, they are more likely to participate actively and collaborate meaningfully with peers.

Collaborative mathematics learning also helps clarify language ambiguities that often confuse students. Kaplan, Fisher, and Rogness (2009) illustrate how lexical ambiguities in terms such as "average," "confidence," and "random" can lead to misconceptions in statistical reasoning. Through peer discussions and guided inquiry, students have opportunities to negotiate meanings and clarify misunderstandings in real-time, which strengthens both their language proficiency and conceptual grasp of mathematics.

Moreover, students benefit from observing multiple problem-solving approaches during group work, which deepens their strategic thinking. Empson (2003) showed how low-performing students gained conceptual understanding of fractions by listening to and interacting with peers during scaffolded discussions. Such findings align with Kazemi and Franke's (2001) assertion that learning within a community of practice fosters generative growth, where students learn not only mathematical content but also how to engage in mathematical discourse.

Importantly, social engagement in math classrooms must be intentionally cultivated. Teachers play a key role in creating conditions that encourage participation from all learners. Fuchs et al. (1998) highlighted how cooperative performance assessments improved both engagement and achievement among diverse student populations. Teachers must be adept at facilitating equitable discussions, mediating group dynamics, and ensuring that all students' voices are heard. Dunn (2005) and Erickson (1986) emphasize the importance of reflective teaching practices that challenge deficit thinking and promote inclusive pedagogies.

Furthermore, long-term instructional change toward socially engaging pedagogy requires supportive institutional structures. Cobb et al. (2003) argue that teachers' instructional practices are shaped not only by individual beliefs but also by school and district-level norms. Professional development programs, such as those explored by Desimone, Smith, and Ueno (2006), are essential in equipping educators with strategies to manage linguistically and culturally diverse classrooms effectively.

Social engagement in the mathematics classroom is not merely about group work or participation—it is about fostering a community of learners who construct meaning together, support one another, and engage deeply with mathematical ideas through language and interaction. For ELLs and culturally diverse learners, this engagement is both a cognitive and an emotional process, rooted in relationships, language, and cultural recognition. As the literature suggests, the

more mathematics instruction is aligned with students' social and linguistic realities, the more empowered and mathematically proficient they become.

Cultural Responsiveness:

Cultural responsiveness in mathematics education refers to the intentional recognition and integration of students' cultural backgrounds, languages, and community experiences into the teaching and learning process. When implemented thoughtfully, it enhances contextual relevance, promotes inclusivity, and fosters a more equitable learning environment (Civil, 2007; Dunn, 2005). Peer-based instructional strategies, such as "math buddies," can be especially effective in promoting cultural responsiveness, as they draw upon shared cultural experiences and vernaculars, allowing learners to make sense of mathematical ideas within familiar sociocultural frames.

Students from linguistically diverse backgrounds, particularly English Language Learners (ELLs), often face challenges in grasping mathematical concepts due to the dual demand of learning a new language while also acquiring abstract mathematical reasoning. Mathematics, while often perceived as a universal language, involves context-bound vocabulary and syntax that may be misinterpreted or misunderstood by ELLs (Goldenberg, 2008; Hoffert, 2009). For instance, words such as "difference," "product," or "average" carry meanings in mathematics that differ significantly from their everyday usage, leading to lexical ambiguity and cognitive confusion (Kaplan, Fisher, & Rogness, 2009). Cultural responsiveness addresses these challenges by validating and leveraging students' home languages and lived experiences as resources for learning, rather than treating them as deficits (Dawe, 1983; Fasi, 1999).

Research in bilingual mathematics education has highlighted the cognitive benefits of allowing students to engage with mathematical content in their native languages. Dawe (1983) and Fasi (1999) both found that bilingual students often reasoned more effectively when allowed to process mathematical ideas in their first language. In culturally responsive classrooms, teachers recognize that language is not merely a medium of instruction but a carrier of cultural knowledge and thought processes (Halliday, 1978; Ferrari, 2004). Thus, math instruction that honors multilingualism and community discourses promotes both comprehension and inclusion.

Culturally responsive teaching also acknowledges the role of sociocultural identity in students' engagement with mathematics. As Civil (2007) notes, understanding the cultural contexts in which students live allows educators to design learning activities that are relevant, meaningful, and aligned with students' everyday lives. For instance, mathematical problems contextualized around local practices, such as farming, construction, or traditional measurement systems, can help students see the value and applicability of mathematics in their communities. These connections not only improve comprehension but also affirm students' identities, fostering a stronger sense of belonging and motivation (Frankenstein, 1995; Forman, 2003).

Franke, Kazemi, and Battey (2007) emphasize the importance of community knowledge in creating equitable mathematics instruction. They advocate for classroom practices that support collaborative learning, discourse, and the co-construction of mathematical meaning. Peer-based models like "math buddies" can be particularly effective in this regard, as they facilitate knowledge-sharing among students from similar cultural or linguistic backgrounds. In such settings, learners are encouraged to articulate their thinking, ask questions in their own dialects or languages, and support each other in understanding complex ideas. These practices are rooted in sociocultural theories of learning, which highlight the importance of social interaction and cultural tools in cognitive development (Erickson, 1986; Cobb, 2007).

Furthermore, culturally responsive mathematics instruction requires teachers to reflect critically on their own beliefs, expectations, and instructional practices. Dunn (2005) argues that engaging pre-service and in-service teachers in critical reflection fosters a disposition to teach for diversity and equity. Teachers must interrogate implicit biases and avoid assuming a one-size-fits-all approach to instruction. Instead, they should adopt flexible pedagogies that respect different ways of knowing, communicating, and problem-solving (Flores, 2007; Ferguson, 1998).

Language-sensitive instruction also plays a crucial role in enhancing cultural responsiveness. Kenney (2005) advocates for the use of literacy strategies in mathematics, emphasizing the importance of teaching students to navigate mathematical language and symbols. This includes not only vocabulary but also the conventions of mathematical

argumentation and reasoning. Research by Kazima (2007) and Kasmer (2013) shows that when students are taught explicitly how to decode and use mathematical language, their understanding and engagement improve significantly.

Cultural responsiveness in mathematics education is not a supplementary approach but a necessary framework for equity and effectiveness. By drawing upon students' cultural resources, promoting language-inclusive strategies, and fostering collaborative learning communities, educators can create mathematics classrooms where all learners have the opportunity to succeed. The role of community-based strategies like "math buddies" underscores the power of peer support grounded in shared cultural and linguistic experiences. As Civil (2007) and Dunn (2005) demonstrate, when students see themselves and their communities reflected in the curriculum, their engagement deepens and their academic potential flourishes.

In classrooms that implemented Math Buddy Teaching, ELLs demonstrated improved problem-solving skills and higher participation in mathematical discussions. These results were consistent across diverse linguistic backgrounds, suggesting the approach's adaptability and effectiveness.

Conclusion:

The Math Buddy Teaching model stands out as a promising and effective approach to improving mathematics instruction, particularly for English Language Learners (ELLs). By integrating peer-assisted learning with language development and culturally responsive teaching practices, this strategy supports students in navigating both the linguistic and conceptual challenges of mathematics. Math Buddy Teaching not only fosters mathematical understanding but also builds learners' confidence, promotes collaboration, and validates the cultural and linguistic assets they bring into the classroom.

Incorporating culturally relevant contexts and encouraging dialogue between peers allows students to engage more meaningfully with mathematical content. When students are paired with peers who share similar backgrounds or who have already acquired key mathematical and language skills, they benefit from more relatable explanations and scaffolded support. This collaborative learning environment helps bridge gaps in language proficiency and content knowledge, making mathematics more accessible and less intimidating for ELLs.

Moreover, the Math Buddy approach aligns with research on equity and inclusive education by emphasizing the value of student agency, community knowledge, and differentiated support. It empowers learners to become both teachers and learners within a shared space, contributing to a classroom culture that respects diversity and encourages active participation.

Given the growing linguistic and cultural diversity in today's classrooms, educators are strongly encouraged to adopt and adapt Math Buddy Teaching in ways that suit their specific contexts. Through intentional implementation and ongoing reflection, this model can transform mathematics instruction into an inclusive, collaborative, and empowering experience for all students. In doing so, schools can take significant steps toward closing opportunity gaps and ensuring that every learner—regardless of language background—has equitable access to high-quality mathematics education.

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